Magnus Sahlgren

Pavia, 11 September 2012

Course web page:

http://www.gavagai.se/distributional\_semantics.php

- Theoretical foundations (*the distributional hypothesis*)
- Basic concepts (co-occurrence matrix, distributional vectors)
- Distributional semantic models (LSA, HAL, Random Indexing)
- Applications (lexical semantics, cognitive modelling, data mining)
- Research questions (*semantic relations, compositionality*)

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#### • What are the underlying assumptions and theories?

- What are the main models, and how do they differ?
- How to build and use a model
- How to evaluate a model
- What can we use the models for?
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#### Theoretical basis The Distributional Hypothesis

Representational framework Vector Space

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Extracting *semantics* from the *distributions* of terms

#### Firth:

"you shall know a word by the company it keeps"

#### Wittgenstein:

"the meaning of a word is its use in language"

#### ?:

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- Linguistics can only deal with what is internal to language
- Linguistic explanans is distributional facts

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# Harris' distributional methodology is the *discovery procedure* by which we can quantify distributional similarities between linguistic entities

But why would such distributional similarities indicate *semantic* similarity? (And what does "meaning" mean anyway?)

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## If linguistics is to deal with meaning, it can only do so through distributional analysis

Differential, not referential

Structuralist legacy — Bloomfield, Saussure

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- Two kinds: syntagmatic and paradigmatic

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Example:

1	drink	coffee
you	sip	tea
they	gulp	cocoa

Syntagmatic relations:

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- Hyponyms (e.g. "dog" / "poodle")
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#### "drink" and "coffee" have a syntagmatic relation if they co-occur

"coffee" and "tea" have a paradigmatic relation if they co-occur with the same *other* words (e.g. "drink")

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Structuralism: Meaning = relations between words
Saussure: Two types of relations: syntagmatic and paradigmatic

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Saussure: Two types of relations: syntagmatic and paradigmatic

#### Extracting semantics from the distributions of terms

Extracting *syntagmatic or paradigmatic relations* between words from *co-occurrences or second-order co-occurrences* 

Extracting semantics from the distributions of terms

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# The Distributional Hypothesis makes sense from a linguistic perspective

Does it also make sense from a cognitive perspective?

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Does it also make sense from a cognitive perspective?

# We (i.e. humans) obviously *can* learn new words based on contextual cues

He filled the wapimuk with the substance, passed it around and we all drunk some

We found a little, hairy wapimuk sleeping behind the tree

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#### We encounter new words everyday...

but rarely ask for definitions

The absence of definitions in normal discourse is a sign of communicative prosperity

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# Abstract terms (Vigliocco et al. 2009) justice, tax, etc.

Concrete terms for which we have no direct experience of the referents aardvark, cyclotron, etc.

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Congenitally blind individuals show normal competence of color terms and visual perception verbs (Landau & Gleitman 1985)

The *cognitive representation* of a word is some abstraction or generalization derived from the contexts in which the word has been encountered (Miller & Charles 1991)

#### A contextual representation may include extra-linguistic contexts

De facto, context is equated with linguistic context

- Practical reason it is easy to collect linguistic contexts (from corpora) and to process them
- Theoretical reason it is possible to investigate the role of linguistic distributions in shaping word meaning

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### Weak Distributional Hypothesis

A quantitative method for semantic analysis and lexical resource induction

Meaning (whatever this might be) is reflected in distribution

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### Strong Distributional Hypothesis

A cognitive hypothesis about the form and origin of semantic representations

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Theoretical basis The Distributional Hypothesis

Representational framework Vector Space



 $A_{2,2} = \begin{array}{c} x & y \\ b \end{array} \begin{bmatrix} (4 & 3) \\ (5 & 6) \end{bmatrix}$ 

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# High-dimensional vector spaces (i.e. dimensionalities on the order of thousands)

Mathematically straightforward

Warning: high-dimensional spaces can be counterintuitive!



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How big must the inner cube be in order to cover 1% of the area of the outer cube?

Answer: 10% of the side length (0.1 imes 0.1=0.01)



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# For 3-dimensional cubes, the inner cube must have $\approx 21\%$ of the side length of the outer cube ( $0.21\times0.21\times0.21\approx0.01)$

For *n*-dimensional cubes, the inner cube must have  $0.01^{\frac{1}{n}}$  of the side length



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#### For $n = 1 \ 000$ that is 99.5%

That is, if the outer 1 000-dimensional cube has sides 2 units long, and the inner 1 000-dimensional cube has sides 1.99 units long, the outer cube will still contain *100 times* more volume

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#### Distributional semantics + vector space

Word Space Models

Distributional semantics + vector space

Word Space Models

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## Word Space

"Vector similarity is the only information present in Word Space: semantically related words are close, unrelated words are distant." (Hinrich Schütze: Word space, 1993)

### Word Space

graphical spreadsheets LCMacintoshes diskette RL. Dos Microsoft Presentation megabytes OS хт interfaces PS compatibles Poget Unix Macs interface desktop Metaphor MIPS SX Macintosh Software dbase modem EISA Sparcetation PC. Adobe server megahertz PCs software Vax compatible printers laptops bytes minicomputers font networked laptop Apple microprocessors Microsystems ROM Macworld scanner mainframe Disk peripherals Seybold computing Application Lotus minicomputer Convex Headstart Computer Compag Sparc Mips midrange Internet disk hackers processors Epson workstations Microprocessor user encryption Interface Merrin microcomputer Amdahl computer handheld Thinking AST Jobs Kapor supercomputer Tandem HP Cupertino computationvector machine algorithms CISC Hillis Atari hardware LB.M. IBM Packard Hewlett Intel users configured NCR facsimile BIS networking supercomputing Digital Micro clones MP Cray processing Sunnyvale Nixdorf Dataquest circuitry systems harnessing Хегох Data microns copiers Applications optical Ricoh transistors Zenith NECFujitsu Microchip Canon Toshiba chip ICL Hitachi microchips Silicon chips micron AMD circuits Devices Strategies Logic silicon microchip Motorola LSI etch bipolar lasers gallium robotics technology technologically lithography Advanced technologies technological

VLSI

(Schütze: Dimensions of Meaning, 1992)

#### Manually defined features

Psychology: Osgood (1950s)

Human ratings over contrastive adjective-pairs

	small – large	bald – furry	docile – dangerous
mouse	2	6	1
rat	2	6	4

#### Manually defined features

#### Psychology: Osgood (1950s)

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Manually defined features

Connectionism, AI: Waltz & Pollack (1980s), Gallant (1990s), Gärdenfors (2000s)

human machine politics ... astronomer +2 -1 -1 ...

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Word Space (A Brief History)
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Manually defined features

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#### Manually defined features

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# Automatic methods: count co-occurrences (c.f. the distributional hypothesis)

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- w are the m (target) word types
- c are the n contexts in the data
- and the cells are word-context co-occurrence frequencies

# $A_{m,n} = \begin{bmatrix} c_1 & c_2 & c_3 & \dots & c_n \\ w_1 & & \\ w_2 & & \\ a_{2,1} & a_{2,2} & a_{2,3} & \dots & a_{2,n} \\ a_{3,1} & a_{3,2} & a_{3,3} & \dots & a_{3,n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ w_m & & a_{m,1} & a_{m,2} & a_{m,3} & \dots & a_{m,n} \end{bmatrix}$

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## **Distributional Vectors**



#### Rows are *n*-dimensional distributional vectors

Words that occur in similar contexts get similar distributional vectors

So how should we define "context"?

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## Words-by-region Matrices

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A region is a text unit (document, paragraph, sentence, etc.)  $r_2 = "I \ drink \ coffee"$ 

Syntagmatic similarity: words that co-occur in the same region

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## Words-by-words Matrices



Paradigmatic similarity: words that co-occur with the same *other* words

Syntagmatic similarity by looking at the individual dimensions

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#### The region within which co-occurrences are collected

- Size
- Direction
- Weighting

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## [I drink very strong]coffee[at the cafe down the street]11111

An entire sentence as a flat context window

#### [I drink very strong] coffee [at the cafe down the street] 1 1 1 1 1 1 1 1 1 1 1

An entire sentence as a flat context window

#### I drink [very strong] coffee [at the] cafe down the street 1 1 1 1 1

A 2+2-sized flat context window

#### [I drink very strong] coffee [at the cafe down] the street 1 2 3 4 4 3 2 1

A 4+4-sized *distance weighted* context window

#### I drink very strong coffee [at the cafe down the street] 1 0.9 0.8 0.7 0.6 0.5

A 0+6-sized distance weighted context window

I [drink very strong] coffee [at the cafe] down the street 1 0 3 0 0 1

A 3+3-sized distance weighted context window that ignores stop words

## Distributional vectors

#### Count how many times each target word occurs in a certain context

*Collect* (a function of) these frequency counts in vectors

[12,0,234,92,1,0,87,525,0,0,1,2,0,8129,1,0,51,0,235...]

And then what?

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## The Meaning of Life



## Vector similarity



## Vector similarity



## Vector similarity






### Minkowski distance: $\left(\sum_{i=1}^{n} |x_i - y_i|^N\right)^{\frac{1}{N}}$

- City-Block (or Manhattan) distance: N = 1
- Euclidean distance: N = 2
- Chebyshev distance:  $N \to \infty$

Scalar product:  $x \cdot y = x_1y_1 + x_2y_2 + \ldots + x_ny_n$ 

Cosine: 
$$\frac{x \cdot y}{|x||y|} = \frac{\sum_{i=1}^{n} x_i y_i}{\sqrt{\sum_{i=1}^{n} x_i^2} \sqrt{\sum_{i=1}^{n} y_i^2}}$$

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### Nearest Neighbors

dog	
dog	1.000000
cat	0.774165
horse	0.668386
fox	0.648134
pet	0.626650
rabbit	0.615840
pig	0.570504
animal	0.566003
mongrel	0.560158
sheep	0.551973
pigeon	0.547442
deer	0.534663
rat	0.531442
bird	0.527370

red	
red	1.000000
yellow	0.824409
white	0.789056
brown	0.723576
grey	0.720103
blue	0.700047
pink	0.672573
black	0.671302
shiny	0.661379
purple	0.633858
striped	0.619801
dark	0.610804
gleam	0.603501
palea	0.595221

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i/PN drink/VB very/AV strong/AJ arabica/NN coffee/NN at/PR the/DT cafe/NN

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- Weight the contexts (optional, but recommended) (e.g. raw co-occurrence frequency, entropy, association measures...)
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